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Solving Ordinary Differential Equations I Nonstiff Problems

E. Hairer
S. P. Nørsett
G. Wanner

Second Revised Edition



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Solving Ordinary Differential Equations 1 Nonstiff Problems

**Karline Soetaert, Jeff Cash, Francesca
Mazzia**



Solving Ordinary Differential Equations 1 Nonstiff Problems:

Solving Ordinary Differential Equations I Ernst Hairer, Syvert P. Nørsett, Gerhard Wanner, 2008-04-03 This book deals with methods for solving nonstiff ordinary differential equations The first chapter describes the historical development of the classical theory and the second chapter includes a modern treatment of Runge Kutta and extrapolation methods Chapter three begins with the classical theory of multistep methods and concludes with the theory of general linear methods The reader will benefit from many illustrations a historical and didactic approach and computer programs which help him/her learn to solve all kinds of ordinary differential equations This new edition has been rewritten and new material has been included

Solving Ordinary Differential Equations: Nonstiff problems Ernst Hairer, 1993 *Ordinary Differential Equations and Integral Equations* C.T.H. Baker, G. Monegato, G. vanden Berghe, 2001-07-04 homepage [sac.cam.ac.uk/na2000/index.html](#)7 Volume Set now available at special set price This volume contains contributions in the area of differential equations and integral equations Many numerical methods have arisen in response to the need to solve real life problems in applied mathematics in particular problems that do not have a closed form solution Contributions on both initial value problems and boundary value problems in ordinary differential equations appear in this volume Numerical methods for initial value problems in ordinary differential equations fall naturally into two classes those which use one starting value at each step one step methods and those which are based on several values of the solution multistep methods John Butcher has supplied an expert's perspective of the development of numerical methods for ordinary differential equations in the 20th century Rob Corless and Lawrence Shampine talk about established technology namely software for initial value problems using Runge Kutta and Rosenbrock methods with interpolants to fill in the solution between mesh points but the slant is new based on the question How should such software integrate into the current generation of Problem Solving Environments Natalia Borovikh and Marc Spijker study the problem of establishing upper bounds for the norm of the n th power of square matrices The dynamical system viewpoint has been of great benefit to ODE theory and numerical methods Related is the study of chaotic behaviour Willy Govaerts discusses the numerical methods for the computation and continuation of equilibria and bifurcation points of equilibria of dynamical systems Arieh Iserles and Antonella Zanna survey the construction of Runge Kutta methods which preserve algebraic invariant functions Valeria Antohe and Ian Gladwell present numerical experiments on solving a Hamiltonian system of H non and Heiles with a symplectic and a nonsymplectic method with a variety of precisions and initial conditions Stiff differential equations first became recognized as special during the 1950s In 1963 two seminal publications laid the foundations for later development Dahlquist's paper on A stable multistep methods and Butcher's first paper on implicit Runge Kutta methods Ernst Hairer and Gerhard Wanner deliver a survey which retraces the discovery of the order stars as well as the principal achievements obtained by that theory Guido Vanden Berghe Hans De Meyer Marnix Van Daele and Tanja Van Hecke construct exponentially fitted Runge Kutta methods with s stages Differential algebraic equations arise

in control in modelling of mechanical systems and in many other fields Jeff Cash describes a fairly recent class of formulae for the numerical solution of initial value problems for stiff and differential algebraic systems Shengtai Li and Linda Petzold describe methods and software for sensitivity analysis of solutions of DAE initial value problems Again in the area of differential algebraic systems Neil Biehn John Betts Stephen Campbell and William Huffman present current work on mesh adaptation for DAE two point boundary value problems Contrasting approaches to the question of how good an approximation is as a solution of a given equation involve i attempting to estimate the actual error i e the difference between the true and the approximate solutions and ii attempting to estimate the defect the amount by which the approximation fails to satisfy the given equation and any side conditions The paper by Wayne Enright on defect control relates to carefully analyzed techniques that have been proposed both for ordinary differential equations and for delay differential equations in which an attempt is made to control an estimate of the size of the defect Many phenomena incorporate noise and the numerical solution of stochastic differential equations has developed as a relatively new item of study in the area Keven Burrage Pamela Burrage and Taketomo Mitsui review the way numerical methods for solving stochastic differential equations SDE s are constructed One of the more recent areas to attract scrutiny has been the area of differential equations with after effect retarded delay or neutral delay differential equations and in this volume we include a number of papers on evolutionary problems in this area The paper of Genna Bocharov and Fathalla Rihan conveys the importance in mathematical biology of models using retarded differential equations The contribution by Christopher Baker is intended to convey much of the background necessary for the application of numerical methods and includes some original results on stability and on the solution of approximating equations Alfredo Bellen Nicola Guglielmi and Marino Zennaro contribute to the analysis of stability of numerical solutions of nonlinear neutral differential equations Koen Engelborghs Tatyana Luzyanina Dirk Roose Neville Ford and Volker Wulf consider the numerics of bifurcation in delay differential equations Evelyn Buckwar contributes a paper indicating the construction and analysis of a numerical strategy for stochastic delay differential equations SDDEs This volume contains contributions on both Volterra and Fredholm type integral equations Christopher Baker responded to a late challenge to craft a review of the theory of the basic numerics of Volterra integral and integro differential equations Simon Shaw and John Whiteman discuss Galerkin methods for a type of Volterra integral equation that arises in modelling viscoelasticity A subclass of boundary value problems for ordinary differential equation comprises eigenvalue problems such as Sturm Liouville problems SLP and Schr dinger equations Liviu Ixaru describes the advances made over the last three decades in the field of piecewise perturbation methods for the numerical solution of Sturm Liouville problems in general and systems of Schr dinger equations in particular Alan Andrew surveys the asymptotic correction method for regular Sturm Liouville problems Leon Greenberg and Marco Marletta survey methods for higher order Sturm Liouville problems R Moore in the 1960s first showed the feasibility of validated solutions of differential equations that is of computing guaranteed

enclosures of solutions Boundary integral equations Numerical solution of integral equations associated with boundary value problems has experienced continuing interest Peter Junghanns and Bernd Silbermann present a selection of modern results concerning the numerical analysis of one dimensional Cauchy singular integral equations in particular the stability of operator sequences associated with different projection methods Johannes Elschner and Ivan Graham summarize the most important results achieved in the last years about the numerical solution of one dimensional integral equations of Mellin type of means of projection methods and in particular by collocation methods A survey of results on quadrature methods for solving boundary integral equations is presented by Andreas Rathsfeld Wolfgang Hackbusch and Boris Khoromski present a novel approach for a very efficient treatment of integral operators Ernst Stephan examines multilevel methods for the h p and hp versions of the boundary element method including pre conditioning techniques George Hsiao Olaf Steinbach and Wolfgang Wendland analyze various boundary element methods employed in local discretization schemes

Solving

Differential Equations in R Karline Soetaert, Jeff Cash, Francesca Mazzia, 2012-06-06 Mathematics plays an important role in many scientific and engineering disciplines This book deals with the numerical solution of differential equations a very important branch of mathematics Our aim is to give a practical and theoretical account of how to solve a large variety of differential equations comprising ordinary differential equations initial value problems and boundary value problems differential algebraic equations partial differential equations and delay differential equations The solution of differential equations using R is the main focus of this book It is therefore intended for the practitioner the student and the scientist who wants to know how to use R for solving differential equations However it has been our goal that non mathematicians should at least understand the basics of the methods while obtaining entrance into the relevant literature that provides more mathematical background Therefore each chapter that deals with R examples is preceded by a chapter where the theory behind the numerical methods being used is introduced In the sections that deal with the use of R for solving differential equations we have taken examples from a variety of disciplines including biology chemistry physics pharmacokinetics Many examples are well known test examples used frequently in the field of numerical analysis

Fundamentals of Ordinary Differential Equations Mohit Chatterjee, 2025-02-20 Fundamentals of Ordinary Differential Equations is a comprehensive guide designed for students researchers and professionals to master ODE theory and applications We cover essential principles advanced techniques and practical applications providing a well rounded resource for understanding differential equations and their real world impact The book offers a multifaceted approach from basic principles to advanced concepts catering to fields like physics engineering biology and economics Mathematical ideas are broken down with step by step explanations examples and illustrations making complex concepts accessible Real world examples throughout each chapter show how ODEs model and analyze systems in diverse disciplines We also explain numerical methods such as Euler s method Runge Kutta and finite differences equipping readers with computational tools for solving ODEs Advanced topics include

bifurcation chaos theory Hamiltonian systems and singular perturbations providing an in depth grasp of ODE topics With chapter summaries exercises glossaries and additional resources *Fundamentals of Ordinary Differential Equations* is an essential reference for students professionals and practitioners across science and engineering fields **Numerical Methods for Ordinary Differential Equations** Alfredo Bellen, Charles W. Gear, Elvira Russo, 2006-11-14 Developments in numerical initial value ode methods were the focal topic of the meeting at L'Aquila which explored the connections between the classical background and new research areas such as differential algebraic equations delay integral and integro differential equations stability properties continuous extensions interpolants for Runge Kutta methods and their applications effective stepsize control parallel algorithms for small and large scale parallel architectures The resulting proceedings address many of these topics in both research and survey papers *Introduction to Precise Numerical Methods* Oliver Aberth, 2007-04-11 Precise numerical analysis may be defined as the study of computer methods for solving mathematical problems either exactly or to prescribed accuracy This book explains how precise numerical analysis is constructed The book also provides exercises which illustrate points from the text and references for the methods presented Clearer simpler descriptions and explanations of the various numerical methods Two new types of numerical problems accurately solving partial differential equations with the included software and computing line integrals in the complex plane **Computational Science – ICCS 2004** Marian Bubak, Geert D. van Albada, Peter M.A. Sloot, Jack Dongarra, 2004-05-25 The International Conference on Computational Science ICCS 2004 held in Krakow Poland June 6-9 2004 was a follow up to the highly successful ICCS 2003 held at two locations in Melbourne Australia and St Petersburg Russia ICCS 2002 in Amsterdam The Netherlands and ICCS 2001 in San Francisco USA As computational science is still evolving in its quest for subjects of investigation and efficient methods ICCS 2004 was devised as a forum for scientists from mathematics and computer science as the basic computing disciplines and application areas interested in advanced computational methods for physics chemistry life sciences engineering arts and humanities as well as computer system vendors and software developers The main objective of this conference was to discuss problems and solutions in all areas to identify new issues to shape future directions of research and to help users apply various advanced computational techniques The event harvested recent developments in computational grids and next generation computing systems tools advanced numerical methods data driven systems and novel application fields such as complex systems nanotechnology physics and population evolution *Modeling of Atmospheric Chemistry* Guy P. Brasseur, Daniel J. Jacob, 2017-06-19 This book presents the fundamental principles mathematical methods and applications of atmospheric chemistry models for graduate students and researchers **Computational Science -- ICCS 2005** V.S. Sunderam, 2005-05-12 The three volume set LNCS 3514 3516 constitutes the refereed proceedings of the 5th International Conference on Computational Science ICCS 2005 held in Atlanta GA USA in May 2005 The 464 papers presented were carefully reviewed and selected from a total of 834 submissions for the main conference and its 21 topical

workshops The papers span the whole range of computational science ranging from numerical methods algorithms and computational kernels to programming environments grids networking and tools These fundamental contributions dealing with computer science methodologies and techniques are complemented by papers discussing computational applications and needs in virtually all scientific disciplines applying advanced computational methods and tools to achieve new discoveries with greater accuracy and speed

Reliability and Availability Engineering Kishor S. Trivedi, Andrea Bobbio, 2017-08-03 Do you need to know what technique to use to evaluate the reliability of an engineered system This self contained guide provides comprehensive coverage of all the analytical and modeling techniques currently in use from classical non state and state space approaches to newer and more advanced methods such as binary decision diagrams dynamic fault trees Bayesian belief networks stochastic Petri nets non homogeneous Markov chains semi Markov processes and phase type expansions Readers will quickly understand the relative pros and cons of each technique as well as how to combine different models together to address complex real world modeling scenarios Numerous examples case studies and problems provided throughout help readers put knowledge into practice and a solutions manual and Powerpoint slides for instructors accompany the book online This is the ideal self study guide for students researchers and practitioners in engineering and computer science

Group Theory and Numerical Analysis Pavel Winternitz, The Workshop on Group Theory and Numerical Analysis brought together scientists working in several different but related areas The unifying theme was the application of group theory and geometrical methods to the solution of differential and difference equations The emphasis was on the combination of analytical and numerical methods and also the use of symbolic computation This meeting was organized under the auspices of the Centre de Recherches Mathematiques Universite de Montreal Canada This volume has the character of a monograph and should represent a useful reference book for scientists working in this highly topical field

State Estimation for Nonlinear Continuous-Discrete Stochastic Systems Gennady Yu. Kulikov, Maria V. Kulikova, 2024-09-06 This book addresses the problem of accurate state estimation in nonlinear continuous time stochastic models with additive noise and discrete measurements Its main focus is on numerical aspects of computation of the expectation and covariance in Kalman like filters rather than on statistical properties determining a model of the system state Nevertheless it provides the sound theoretical background and covers all contemporary state estimation techniques beginning at the celebrated Kalman filter including its versions extended to nonlinear stochastic models and till the most advanced universal Gaussian filters with deterministically sampled mean and covariance In particular the authors demonstrate that when applying such filtering procedures to stochastic models with strong nonlinearities the use of adaptive ordinary differential equation solvers with automatic local and global error control facilities allows the discretization error and consequently the state estimation error to be reduced considerably For achieving that the variable stepsize methods with automatic error regulation and stepsize selection mechanisms are applied to treating moment differential equations arisen

The implemented discretization error reduction makes the self adaptive nonlinear Gaussian filtering algorithms more suitable for application and leads to the novel notion of accurate state estimation. The book also discusses accurate state estimation in mathematical models with sparse measurements. Of special interest in this regard it provides a means for treating stiff stochastic systems which are often encountered in applied science and engineering being exemplified by the Van der Pol oscillator in electrical engineering and the Oregonator model of chemical kinetics. Square root implementations of all Kalman like filters considered and explored in this book for state estimation in ill conditioned continuous discrete stochastic systems attract the authors particular attention. This book covers both theoretical and applied aspects of numerical integration methods including the concepts of approximation convergence stiffness as well as of local and global errors suitably for applied scientists and engineers. Such methods serve as a basis for the development of accurate continuous discrete extended unscented cubature and many other Kalman filtering algorithms including the universal Gaussian methods with deterministically sampled expectation and covariance as well as their mixed type versions. The state estimation procedures in this book are presented in the fashion of complete pseudo codes which are ready for implementation and use in MATLAB or in any other computation platform. These are examined numerically and shown to outperform traditional variants of the Kalman like filters in practical prediction filtering tasks including state estimations of stiff and or ill conditioned continuous discrete nonlinear stochastic systems.

Time Parallel Time Integration Martin J. Gander, Thibaut Lunet, 2024-10-15

Predicting the future is a difficult task but as with the weather it is possible with good models. But how does one predict the far future before the near future is known? Time parallel time integration also known as PinT. Parallel in Time methods aim to predict the near and far future simultaneously. In this self contained book the first on the topic readers will find a comprehensive and up to date description of methods and techniques that have been developed to do just this. The authors describe the four main classes of PinT methods: shooting type methods, waveform relaxation methods, time parallel multigrid methods and direct time parallel methods. In addition they provide historical background for each of the method classes, complete convergence analyses for the most representative variants of the methods in each class and illustrations and runnable MATLAB code. An ideal introduction to this exciting and very active research field. *Time Parallel Time Integration* can be used for independent study or for a graduate course.

Numerical Methods and Optimization Jean-Pierre Corriou, 2022-01-04. This text covering a very large span of numerical methods and optimization is primarily aimed at advanced undergraduate and graduate students. A background in calculus and linear algebra are the only mathematical requirements. The abundance of advanced methods and practical applications will be attractive to scientists and researchers working in different branches of engineering. The reader is progressively introduced to general numerical methods and optimization algorithms in each chapter. Examples accompany the various methods and guide the students to a better understanding of the applications. The user is often provided with the opportunity to verify their results with complex

programming code Each chapter ends with graduated exercises which furnish the student with new cases to study as well as ideas for exam homework problems for the instructor A set of programs made in MatlabTM is available on the author's personal website and presents both numerical and optimization methods

Digital Simulation in Electrochemistry Dieter Britz, Jörg Strutwolf, 2016-05-09 This book explains how the partial differential equations pdes in electroanalytical chemistry can be solved numerically It guides the reader through the topic in a very didactic way by first introducing and discussing the basic equations along with some model systems as test cases systematically Then it outlines basic numerical approximations for derivatives and techniques for the numerical solution of ordinary differential equations Finally more complicated methods for approaching the pdes are derived The authors describe major implicit methods in detail and show how to handle homogeneous chemical reactions even including coupled and nonlinear cases On this basis more advanced techniques are briefly sketched and some of the commercially available programs are discussed In this way the reader is systematically guided and can learn the tools for approaching his own electrochemical simulation problems This new fourth edition has been carefully revised updated and extended compared to the previous edition

Lecture Notes in Physics Vol 666 It contains new material describing migration effects as well as arrays of ultramicroelectrodes It is thus the most comprehensive and didactic introduction to the topic of electrochemical simulation

A Graduate Introduction to Numerical Methods Robert M. Corless, Nicolas Fillion, 2013-12-12 This book provides an extensive introduction to numerical computing from the viewpoint of backward error analysis The intended audience includes students and researchers in science engineering and mathematics The approach taken is somewhat informal owing to the wide variety of backgrounds of the readers but the central ideas of backward error and sensitivity conditioning are systematically emphasized The book is divided into four parts Part I provides the background preliminaries including floating point arithmetic polynomials and computer evaluation of functions Part II covers numerical linear algebra Part III covers interpolation the FFT and quadrature and Part IV covers numerical solutions of differential equations including initial value problems boundary value problems delay differential equations and a brief chapter on partial differential equations The book contains detailed illustrations chapter summaries and a variety of exercises as well some Matlab codes provided online as supplementary material I really like the focus on backward error analysis and condition This is novel in a textbook and a practical approach that will bring welcome attention

Lawrence F Shampine *A Graduate Introduction to Numerical Methods and Backward Error Analysis* has been selected by Computing Reviews as a notable book in computing in 2013 Computing Reviews Best of 2013 list consists of book and article nominations from reviewers CR category editors the editors in chief of journals and others in the computing community

Computational Science - ICCS 2006 Vassil N. Alexandrov, G. Dick van Albada, Peter M.A. Sloot, J. J. Dongarra, 2006-05-10 This is Volume I of the four volume set LNCS 3991 3994 constituting the refereed proceedings of the 6th International Conference on Computational Science ICCS 2006 The 98 revised full papers and 29 revised poster papers of the main track presented

together with 500 accepted workshop papers were carefully reviewed and selected for inclusion in the four volumes The coverage spans the whole range of computational science

Mathematical Modeling and Simulation Kai Velten, Dominik M. Schmidt, Katrin Kahlen, 2024-10-07 Learn to use modeling and simulation methods to attack real world problems from physics to engineering from life sciences to process engineering Reviews of the first edition 2009 Perfectly fits introductory modeling courses and is an enjoyable reading in the first place Highly recommended Zentralblatt MATH European Mathematical Society 2009 This book differs from almost all other available modeling books in that the authors address both mechanistic and statistical models as well as hybrid models The modeling range is enormous SIAM Society of Industrial and Applied Mathematics USA 2011 This completely revised and substantially extended second edition answers the most important questions in the field of modeling What is a mathematical model What types of models do exist Which model is appropriate for a particular problem What are simulation parameter estimation and validation What kind of mathematical problems appear and how can these be efficiently solved using professional free of charge open source software The book addresses undergraduates and practitioners alike Although only basic knowledge of calculus and linear algebra is required the most important mathematical structures are discussed in sufficient detail ranging from statistical models to partial differential equations and accompanied by examples from biology ecology economics medicine agricultural chemical electrical mechanical and process engineering About 200 pages of additional material include a unique chapter on virtualization Crash Courses on the data analysis and programming languages R and Python and on the computer algebra language Maxima many new methods and examples scattered throughout the book and an update of all software related procedures and a comprehensive book software providing templates for typical modeling tasks in thousands of code lines The book software includes GmLinux an operating system specifically designed for this book providing preconfigured and ready to use installations of OpenFOAM Salome FreeCAD CfdOF workbench ParaView R Maxima wxMaxima Python Rstudio Quarto Markdown and other free of charge open source software used in the book

Model-Based Hypothesis Testing in Biomedicine Rikard Johansson, 2017-10-03 The utilization of mathematical tools within biology and medicine has traditionally been less widespread compared to other hard sciences such as physics and chemistry However an increased need for tools such as data processing bioinformatics statistics and mathematical modeling have emerged due to advancements during the last decades These advancements are partly due to the development of high throughput experimental procedures and techniques which produce ever increasing amounts of data For all aspects of biology and medicine these data reveal a high level of inter connectivity between components which operate on many levels of control and with multiple feedbacks both between and within each level of control However the availability of these large scale data is not synonymous to a detailed mechanistic understanding of the underlying system Rather a mechanistic understanding is gained first when we construct a hypothesis and test its predictions experimentally Identifying interesting predictions that

are quantitative in nature generally requires mathematical modeling. This in turn requires that the studied system can be formulated into a mathematical model such as a series of ordinary differential equations where different hypotheses can be expressed as precise mathematical expressions that influence the output of the model. Within specific sub domains of biology the utilization of mathematical models have had a long tradition such as the modeling done on electrophysiology by Hodgkin and Huxley in the 1950s. However it is only in recent years with the arrival of the field known as systems biology that mathematical modeling has become more commonplace. The somewhat slow adaptation of mathematical modeling in biology is partly due to historical differences in training and terminology as well as in a lack of awareness of showcases illustrating how modeling can make a difference or even be required for a correct analysis of the experimental data. In this work I provide such showcases by demonstrating the universality and applicability of mathematical modeling and hypothesis testing in three disparate biological systems. In Paper II we demonstrate how mathematical modeling is necessary for the correct interpretation and analysis of dominant negative inhibition data in insulin signaling in primary human adipocytes. In Paper III we use modeling to determine transport rates across the nuclear membrane in yeast cells and we show how this technique is superior to traditional curve fitting methods. We also demonstrate the issue of population heterogeneity and the need to account for individual differences between cells and the population at large. In Paper IV we use mathematical modeling to reject three hypotheses concerning the phenomenon of facilitation in pyramidal nerve cells in rats and mice. We also show how one surviving hypothesis can explain all data and adequately describe independent validation data. Finally in Paper I we develop a method for model selection and discrimination using parametric bootstrapping and the combination of several different empirical distributions of traditional statistical tests. We show how the empirical log likelihood ratio test is the best combination of two tests and how this can be used not only for model selection but also for model discrimination. In conclusion mathematical modeling is a valuable tool for analyzing data and testing biological hypotheses regardless of the underlying biological system. Further development of modeling methods and applications are therefore important since these will in all likelihood play a crucial role in all future aspects of biology and medicine especially in dealing with the burden of increasing amounts of data that is made available with new experimental techniques.

Användandet av matematiska verktyg har inom biologi och medicin traditionellt sett varit mindre utbredd jämfört med andra områden inom naturvetenskaperna som fysik och kemi. Ett stort behov av verktyg som databehandling, bioinformatik, statistik och matematisk modellering har därför framträtt framför framstegen under de senaste decennierna. Dessa framsteg är delvis ett resultat av utvecklingen av storskaliga datainsamlingstekniker. Inom alla områden av biologi och medicin så har dessa data avslöjat en hög nivå av interkonnekterhet mellan komponenter, verkansamma på många kontrollnivåer och med flera terkopplingar både mellan och inom varje nivå av kontroll. Tillgången till storskaliga data är emellertid inte synonymt med en detaljerad mekanistisk förståelse för det underliggande systemet. Snarare uppnås en mekanisk förståelse först när vi bygger en hypotes vars prediktioner vi kan testa experimentellt. Att

identifiera intressanta prediktioner som är av kvantitativ natur kräver generellt sett matematisk modellering. Detta kräver i sin tur att det studerade systemet kan formuleras till en matematisk modell såsom en serie ordinarie differentialekvationer där olika hypoteser kan uttryckas som precisa matematiska uttryck som påverkar modellens output. Inom vissa delområden av biologin har utnyttjandet av matematiska modeller haft en lång tradition såsom den modellering gjord inom elektrofysiologi av Hodgkin och Huxley på 1950-talet. Det är emellertid just på senare år med ankomsten av fältet systembiologi som matematisk modellering har blivit ett vanligt inslag. Den nyligen gott om långsamma adapteringen av matematisk modellering inom biologi är bl.a. grundad i historiska skillnader i terminologi samt brist på medvetenhet om exempel som illustrerar hur modellering kan ge skillnad och faktiskt ofta är ett krav för en korrekt analys av experimentella data. I detta arbete tillhandahåller jag sådana exempel och demonstrerar den matematiska modelleringens och hypotestestningens allmännyttighet och tillämpbarhet i tre olika biologiska system. I Arbete II visar vi hur matematisk modellering är nödvändig för en korrekt tolkning och analys av dominant negativ inhiberingsdata vid insulinsignalering i primära humana adipocyter. I Arbete III använder vi modellering för att bestämma transporthastigheter över cellkärnmembranet i jästceller och vi visar hur denna teknik överlappar traditionella kurvpassningsmetoder. Vi demonstrerar också förgävan om populationsheterogenitet och behovet av att ta hänsyn till individuella skillnader mellan celler och befolkningen som helhet. I Arbete IV använder vi matematisk modellering för att förkasta tre hypoteser om hur fenomenet facilitering uppstår i pyramidala nervceller hos råtta och mus. Vi visar också hur en verlevande hypotes kan beskriva all data inklusive oberoende valideringsdata. Slutligen utvecklar vi i Arbete I en metod för modellselektion och modelldiskriminering med hjälp av parametrisk bootstrapping samt kombinationen av olika empiriska fördelningar av traditionella statistiska tester. Vi visar hur det empiriska log-likelihood ratio testet är den bästa kombinationen av två tester och hur testet är applicerbart inte bara för modellselektion utan också för modelldiskriminering. Sammanfattningsvis är matematisk modellering ett värdefullt verktyg för att analysera data och testa biologiska hypoteser oavsett underliggande biologiskt system. Vidare utveckling av modelleringsmetoder och tillämpningar är därför viktigt eftersom dessa sannolikt kommer att spela en avgörande roll i framtiden för biologi och medicin särskilt när det gäller att hantera belastningen från ökande datamängder som blir tillgänglig med nya experimentella tekniker.

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